

- 1) a homomorphism if for all $v_i \in V, i \in \underline{n} : \tau[v_1, \dots, v_n] = [\tau(v_1), \dots, \tau(v_n)]$;
- 2) an isomorphism if τ is bijective in addition;
- 3) an automorphism if $V_1 = V_2$ and τ is an isomorphism.

For the sake of convenience we introduce the following notation. Let V be an n -Lie algebra and $U_i, i \in \underline{n}$, be subspaces of V . We shall denote by $[U_1, \dots, U_n]$ the subspace of V which is spanned by the elements of the form $[u_1, \dots, u_n], u_i \in U_i$.

Definition: Let V be an n -Lie algebra.

- 1) A subspace U of V is called an n -Lie subalgebra if $[U, \dots, U] \subseteq U$.
- 2) A subspace I of V is called an ideal of V if $[I, V, \dots, V] \subseteq I$.
- 3) V is called simple if $[V, \dots, V] \neq \{0\}$ and has no ideals except itself and $\{0\}$.

Let V be an n -Lie algebra. Then

$$C(V) := \{u \in V \mid [v_1, \dots, v_{n-1}, u] = 0, \forall v_i \in V, i \in \underline{n-1}\},$$

the centre of V , is an ideal of V . In the following we give more examples of ideals and subalgebras.

Example 1.1.4: The n -Lie algebra V in Example 1.1.3 has Kv_0 as an ideal. It is clear that the nonzero ideals of V are exactly the subspaces of V which include Kv_0 .

Example 1.1.5: The subspace $\mathbb{R}[x_1, \dots, x_n]$ of polynomial functions in the n -Lie algebra $C^\infty(\mathbb{R}^n)$ is closed with respect to the n -Lie product, therefore an n -Lie subalgebra of $C^\infty(\mathbb{R}^n)$. Moreover one can verify that for each i the set of all polynomial functions of the form $x_i f, f \in \mathbb{R}[x_1, \dots, x_n]$ is a subalgebra of $\mathbb{R}[x_1, \dots, x_n]$.

In the following proposition we list some simple properties of ideals. We shall give no proofs.

Proposition 1.1.1: Let V be an n -Lie algebra over K and I, J be two ideals of V . Then the following are valid.

- 1) $I + J$ is an ideal of V .