

if at least two of the $2n - 1$ vectors are from I , we have always $a = b = 0$. In any case, $a = b$. Therefore V is an n -Lie algebra. Moreover, it is clear according to the definition that I is an ideal and V_1 a subalgebra of V . \square

Remark 2.2: A natural question is whether there exists an $\text{Inder}(V_1)$ -module I with the property (2.4). The answer to this question is 'yes'. Indeed, let I be a space with $\dim(I) = \dim(V_1) = m$. Let $\{e_i\}_{i \in \underline{m}}$ be a basis of V_1 and $\{f_i\}_{i \in \underline{m}}$ of I . For $v_i \in V_1$, $i \in \underline{n-1}$, let $\rho(\text{ad}(v_1, \dots, v_{n-1}))$ be the endomorphism of I , for which the matrix relative to the basis $\{f_i\}_{i \in \underline{m}}$ equals the matrix for $\text{ad}(v_1, \dots, v_{n-1})$ relative to the basis $\{e_i\}_{i \in \underline{m}}$. Obviously $\rho(\text{ad}(v_1, \dots, v_{n-1}))$ is well defined and it gives rise to a representation of $\text{Inder}(V_1)$ in I . Moreover we have

$$\begin{aligned} & \rho(\text{ad}(u_1, \dots, u_{n-2}, [v_1, \dots, v_n])) \\ &= \sum_{i=1}^n (-1)^{n-i} \rho(\text{ad}(v_1, \dots, \widehat{v_i}, \dots, v_n)) \rho(\text{ad}(u_1, \dots, u_{n-2}, v_i)). \end{aligned}$$