reductive if and only if it is a direct sum of its centre and the semisimple subalgebra $[V, \cdots, V]$.