$$F = \sum_{n=1}^{\infty} \varphi_m(\tau, z)\, e^{2\pi i n \tau'} \in S_k(\Gamma_2)$$

$$G = \sum \psi_m(\ )$$

$$D_{F,G}(s) = \sum_{1}^{\infty} \frac{\langle \varphi_m , \psi_m \rangle}{m^s} \in J^{cusp}_{k,m}(Sl_2(\mathbb{A}))$$

$F \neq G \in S^{Maaß}$

1) $D_{F,F}(s) = *$ Andrianov Zetafct.

2) $D_{F,G}(s)$ merom. continu., funct. equation, $D_{F,F}(s)$ has exactly two poles

3) $D_{F,F}(s) \neq$ And. if $F \in$ Compl. of $S^{Maaß}$.

4) $D_{F,G}(s) =$ Andr.-Zetaf. of F

F arbitrary

$G \in S^{Maaß}$

$\alpha \in K$

$$\zeta_K(m) = \pi^{?} \prod_{i=1}^{r} Log_m(\alpha_i)$$

$$\zeta_a(3) = \sum \frac{z^n}{n^3}\Big|_{z=1} \quad \sum_{1}^{\infty} \frac{z^n}{n^m}$$

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