

between  $S^n$  and  $\mathbb{R}^n$  for  $n > 1$ , therefore one has to use here other ways to translate topological problems into algebraic ones. One of the possible concepts is given by higher dimensional homotopy groups  $\pi_n(X, x_0)$  based on homotopy classes of maps  $c : E^n \rightarrow X$  with  $c(S^{n-1}) = \{x_0\}$ . Then we have  $\pi_n(S^n) = \mathbb{Z}$  and  $\pi_n(E^{n+1}) = 0$  and  $\pi_n(\mathbb{R}^n) = 0$ , and this implies the following generalizations of Cor. 1 and 2 on pp. 18 and 19:

No retraction-theorem: There exists no continuous map  $f : E^{n+1} \rightarrow S^n$  with  $\forall x \in S^n \quad f(x) = x$  ( $n = 0, 1, \dots$ )

Brower fixed point theorem: Each continuous map  $f : E^n \rightarrow E^n$  has at least one fixed point  $x \in E^n$  (i.e.  $f(x) = x$ )

There are still other tools in algebraic topology which allow to prove results like  $\mathbb{R}^n \not\cong \mathbb{R}^m$  for  $n \neq m$ ; and many, many, many other theorems about topological spaces and continuous maps.

Appendix 1: Solutions of the problems of the first hourly.

1). Prove that each subspace of a Hausdorff space is Hausdorff.

Let  $X$  be a Hausdorff space and  $A \subset X$ . We have to show that any two different points  $x_1$  and  $x_2$  in  $A$  can be separated by disjoint neighborhoods in  $A$ . Since  $x_1, x_2 \in X$  we have open subsets  $U_{x_1}$  and  $U_{x_2}$  in  $X$  with  $x_1 \in U_{x_1}$  and  $x_2 \in U_{x_2}$  and  $U_{x_1} \cap U_{x_2} = \emptyset$ . Then  $V_{x_1} = U_{x_1} \cap A$  and  $V_{x_2} = U_{x_2} \cap A$  are open in  $A$ ,  $x_1 \in V_{x_1}$ ,  $x_2 \in V_{x_2}$  and we have clearly  $V_{x_1} \cap V_{x_2} = \emptyset$ .  $V_{x_1}$  and  $V_{x_2}$  are the required neighborhoods. Hence  $A$  is Hausdorff.